



Origin of High-Temperature Superconductivity

Nature's great puzzle

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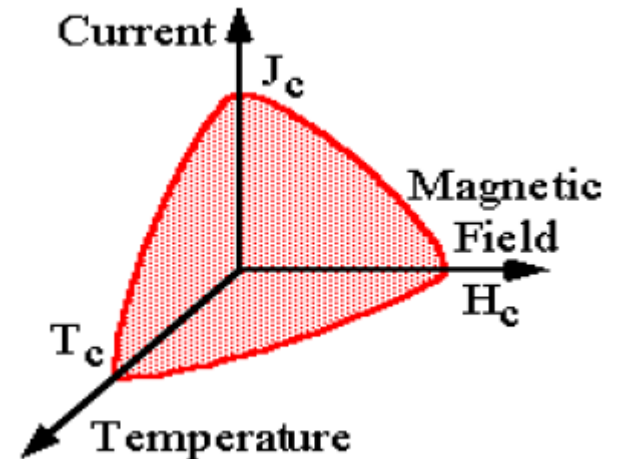
Basic characteristics of superconductors:

- **Perfect electrical conduction**

Kamerlingh Onnes (1911)

capacity of carrying an electrical current without energy loss

$$R = 0, \text{ if } T < T_c \text{ and } J < J_c .$$



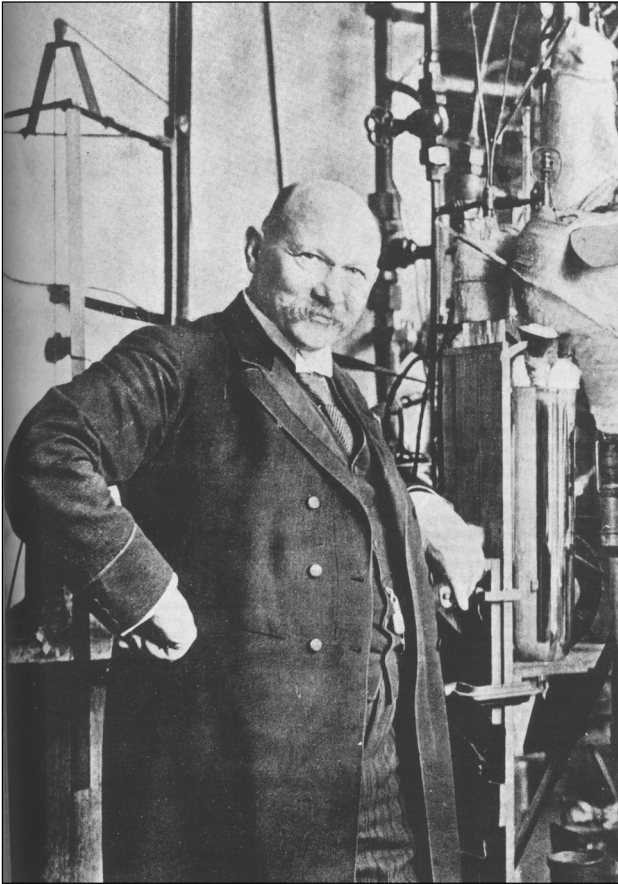
- **Perfect diamagnetism**

W. Meissner and R. Ochsenfeld (1933)

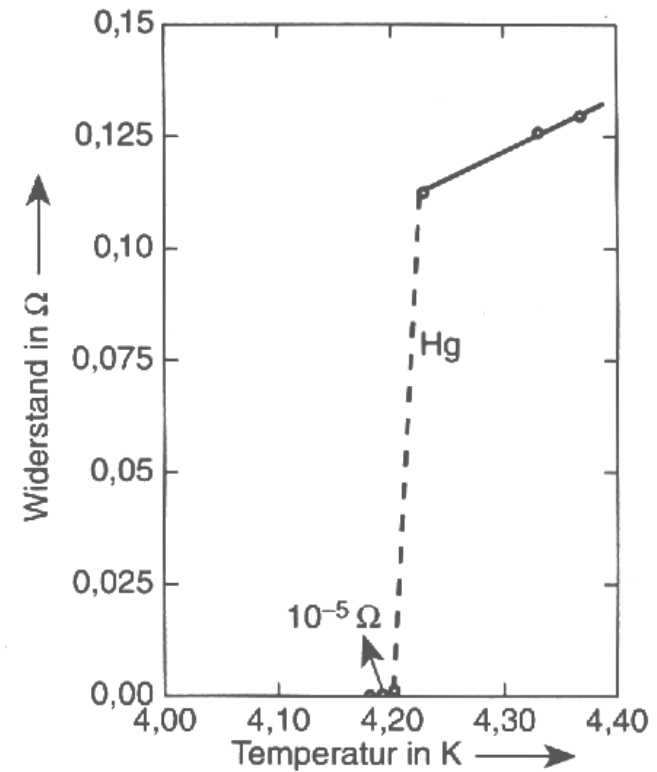
ability to expel a magnetic field

$$\text{if } H < H_c$$

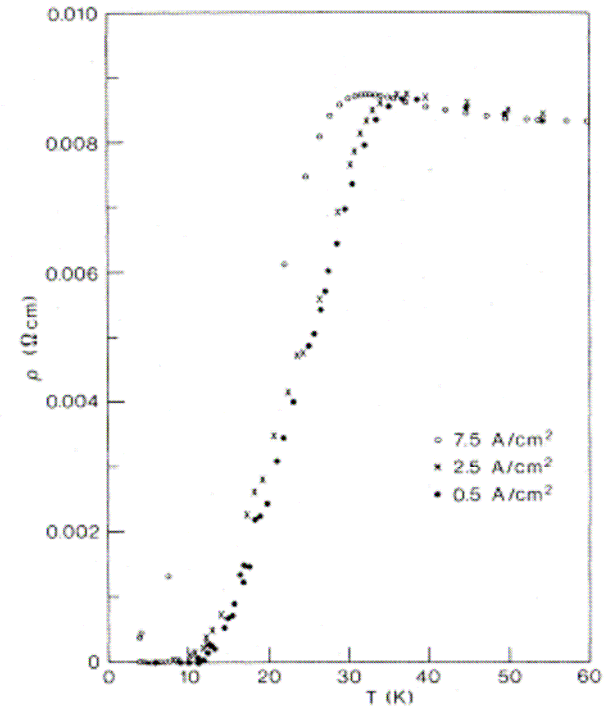
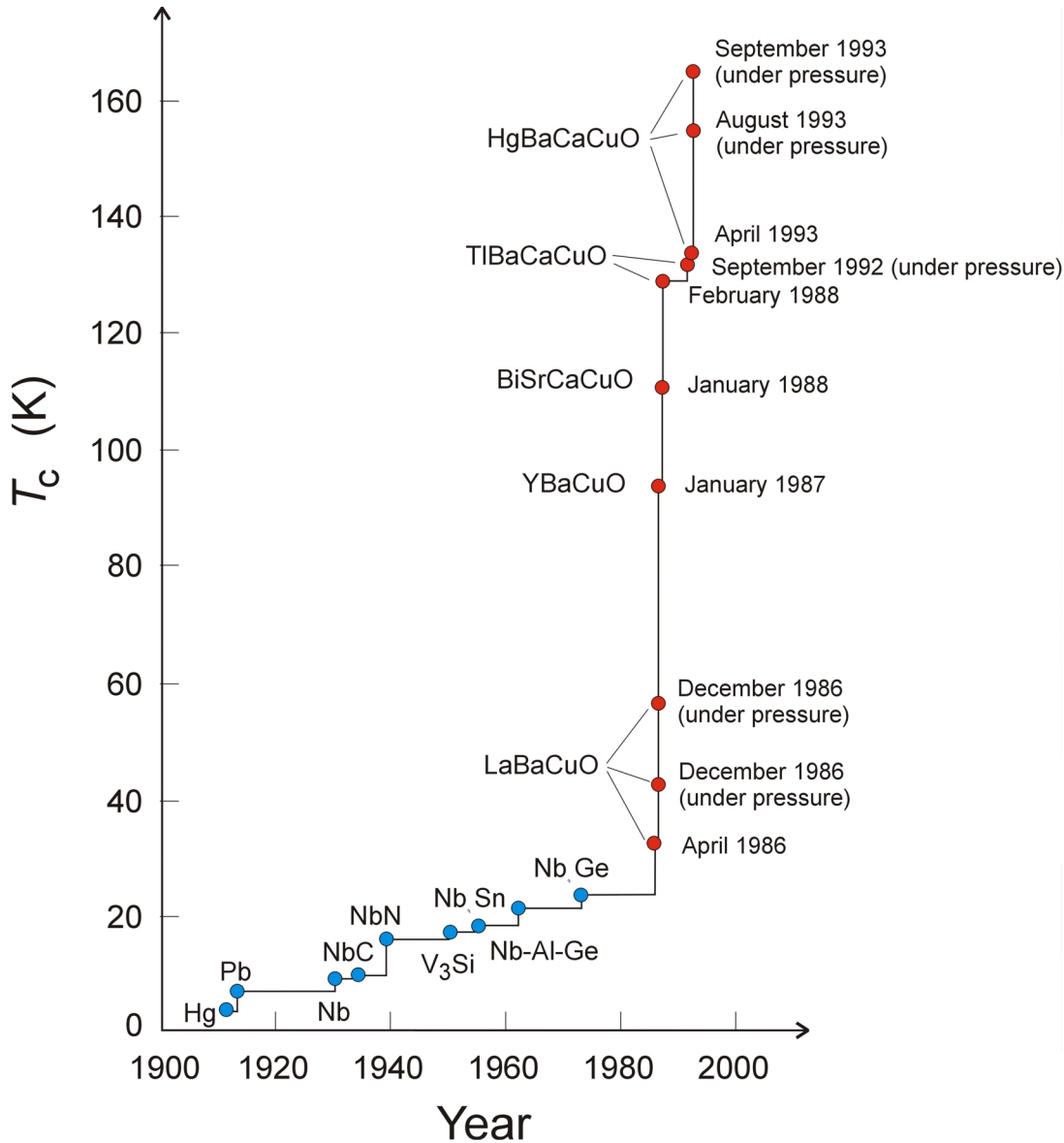
The discovery of low-temperature superconductors



Heike Kamerlingh Onnes (1911)



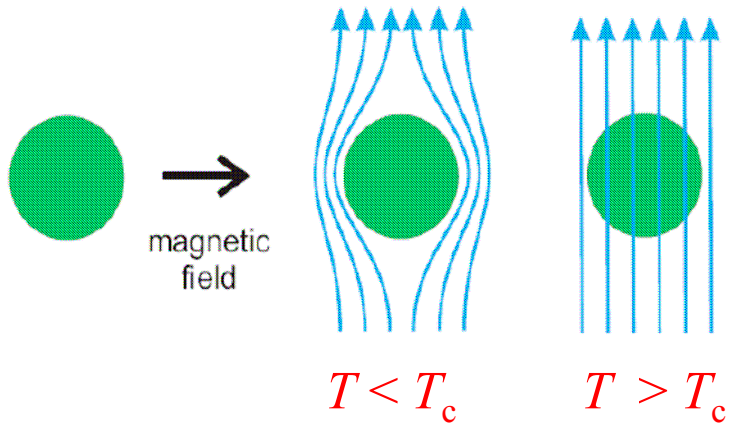
The discovery of high-temperature superconductors (HTS)



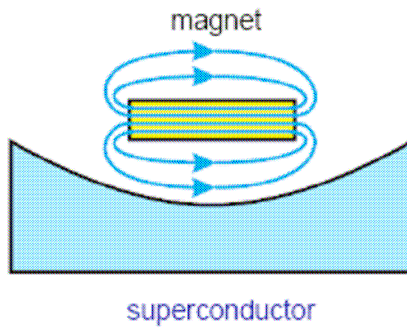
Bednorz and Mueller (1986)



The Meissner effect:



Levitation of a magnet:



BCS Theory of Superconductivity

Phys. Rev. **108**, 1175 (1957).



The Nobel Prize in Physics 1972



John Bardeen



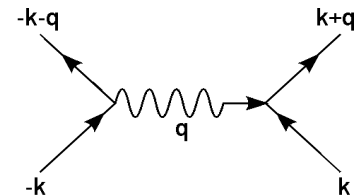
Leon Neil Cooper



John Robert Schrieffer

The BCS pairing glue in conventional superconductors:

Phonon-mediated attractive interaction
between electrons

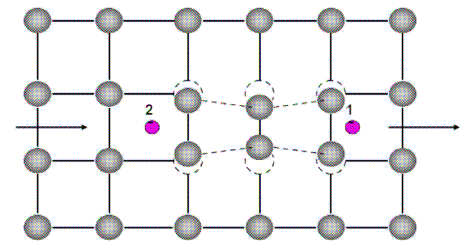


BCS Theory: *How to glue the electrons into pairs against their Coulomb repulsion?*

Cooper pairs are formed by two electrons, which overcome their Coulomb repulsion and experience an attraction through phonon exchanges

Classical analogy: hard balls rolling on a spring mattress.

QM description:



Below T_c , electrons are bound into Cooper pairs(bosons) of anti-parallel spins.
Energy gap: a finite amount of energy is required to break the pair.

$$\Delta(T) > 0, \quad T < T_c$$

Any number of these pairs could have the same energy state (bosonic condensation).
This macroscopic quantum coherent state can be described by:

BCS pair wave function,

$$\Psi(\mathbf{k}) = |\Psi| e^{i\phi} \propto \Delta(\mathbf{k})$$

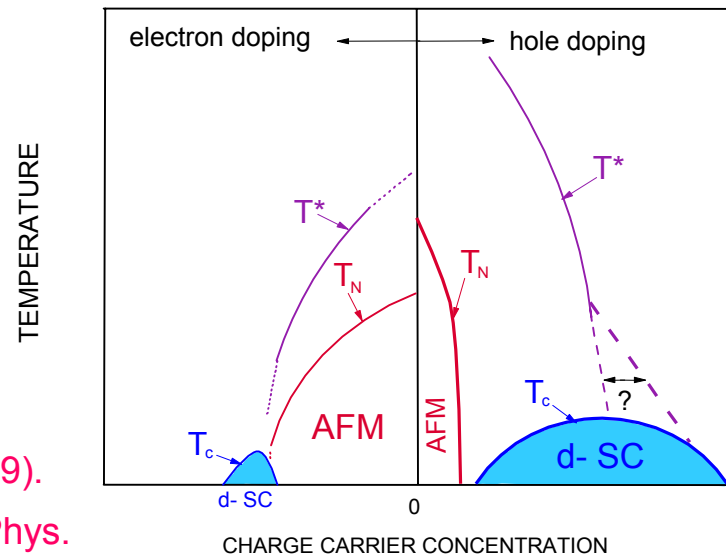
The *normal state* in cuprate superconductors is definitely not normal !!

Outstanding issues to be settled:

- origin of pseudogap
- preformed Cooper pairs
- nanometer scale charge inhomogeneity
- anomalous transport properties
- doping effect (doping-induced evolution from a non-FL to FL behavior)
- - - - -

T. Timusk and B. Statt, *Rep. Prog. Phys.* **62**, 61 (1999).
A. Damascelli, Z. Hussain and Z-X Shen *Rev. Mod. Phys.* **75**, 473 (2003).

Phase diagram of cuprate superconductors

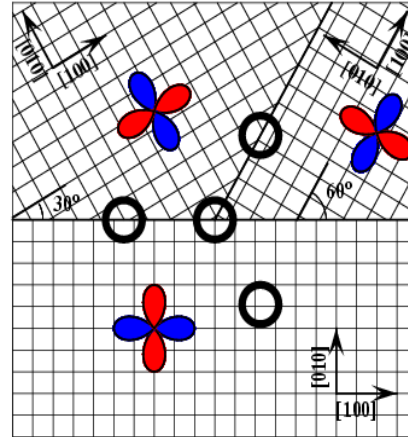


The superconducting state:

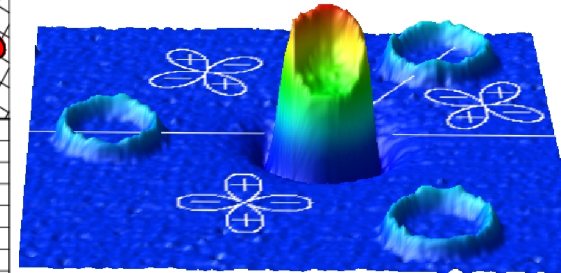
- d-wave pairing symmetry has been observed in both electron- and hole-doped cuprate superconductors.
- The d-wave pair state is robust against TRSB, and a large variation in temperature and doping.
- Experiments probing the nature of nodal excitations in 2D d-wave superconductors support BCS in the context of the FL formalism.
- No consensus on the microscopic pairing mechanism. Contenders include:

- *superexchange interaction*
- *AF magnetic fluctuations*
- *phonons*

Tricrystal geometry



Scanning SQUID microscope image



C.C. Tsuei et al., PRL 73, 593 (1994)

C.C. Tsuei and J.R. Kirtley, Rev. Mod. Phys. 72, 969 (2000)



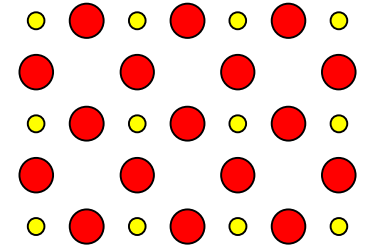
Origin of High-Temperature Superconductivity

Nature's great puzzle

How to piece together the puzzle?

pick the right pieces!!

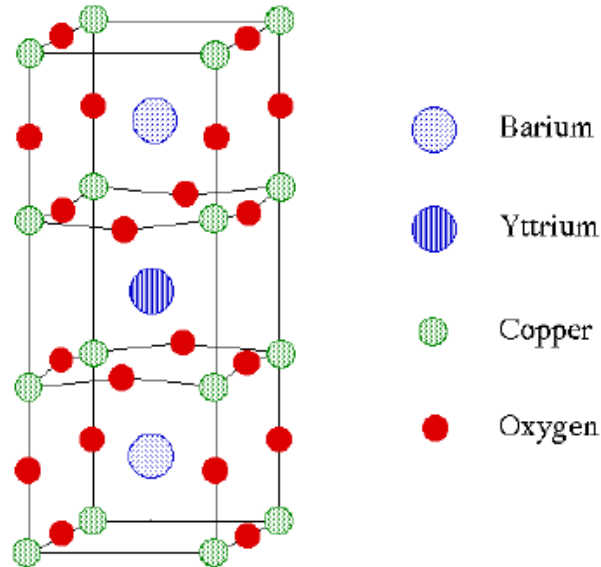
Key findings about HTS:



- *2D layered structure, strongly correlated electron systems*
- *doping effects (on T_c , n_s , - - - -)*
- *d-wave pairing symmetry*
- *anomalous normal state (T^* , ρ , R_H , - - -),
d-wave like pseudogap in the single particle excitation spectrum below T^**
- *doping-dependent isotope effects*
- *nano-scale C_{4v} symmetry-breaking in electronic structure*
- *- - - -*



An example of the high-temperature superconductors:

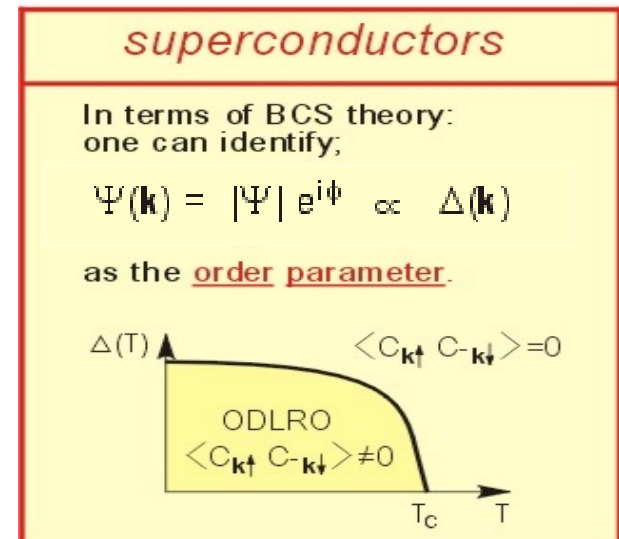
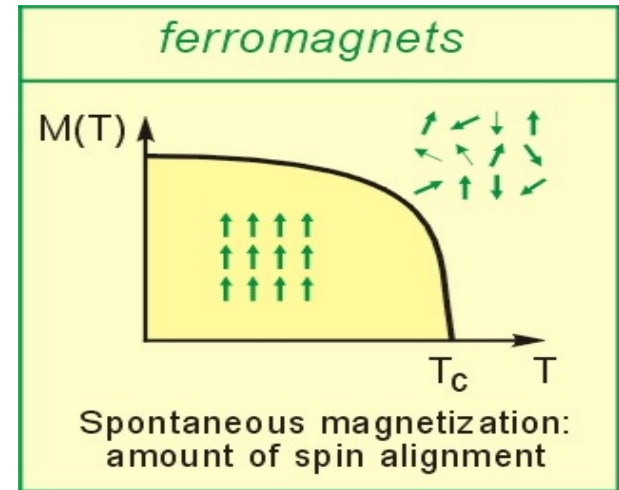


$$T_c \sim 100\text{K}$$

Note: Cu-O square lattice with Cu-O-Cu buckling bonds

Symmetry Breaking and Order Parameter

- Big Bang, Parity Nonconservation
Ferromagnetic
Superconducting Phase transitions
- Full Symmetry Group: G
 Symmetry Breaking $\rightarrow H, H \subset G$
- Order Parameter: a measure of the amount of symmetry breaking

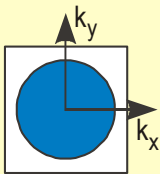

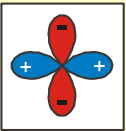
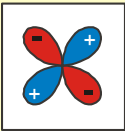


SUPERCONDUCTIVITY

A state of spontaneously broken symmetry

$$T > T_c: G = \underbrace{G_{\text{xtl}}}_{\text{crystal}} \times \underbrace{R_{\text{spin}}}_{\text{spin rotation}} \times \underbrace{U(1)}_{\text{gauge}} \times \underbrace{T}_{\text{time reversal}}$$

$T < T_c$: The global gauge symmetry $U(1)$ is always broken.

Group-theoretic notation	A_{1g}	A_{2g}	B_{1g}	B_{2g}
Order parameter basis function	constant	$xy(x^2-y^2)$	x^2-y^2	xy
Wave function name	s-wave	g	$d_{x^2-y^2}$	d_{xy}
Schematic representation of $\Delta(\mathbf{k})$ in B.Z.				

- Conventional superconductors: s-wave, only $U(1)$ broken at T_c
- **Unconventional superconductors:** such as d-wave

OP has nodes ($\Delta = 0$ on FS)
 $\Delta(\mathbf{k})$ changes its sign as a function of \mathbf{k}

Phase-sensitive test for a definitive determination of pairing symmetry

Phase-sensitive experiment:

Pair tunneling + Flux quantization

$$I_s = -|I_c| \sin \Delta\varphi_{ij} = |I_c| \sin(\Delta\varphi_{ij} + \pi) \quad I_c \propto \Psi_i \Psi_j^* \propto e^{i(\varphi_i - \varphi_j)}$$

$$\Phi_a + I_s L + \frac{\Phi_0}{2\pi} \sum_{ij} \Delta\varphi_{ij} = n\Phi_0$$

$$U(\Phi, \Phi_a) = \frac{\Phi_0^2}{2\pi} \left\{ \left(\frac{\Phi + \Phi_a}{\Phi_0} \right)^2 - \frac{L|I_c|}{\pi\Phi_0} \cos \left[\left(\frac{2\pi\Phi}{\Phi_0} \right) + \theta \right] \right\}; \quad \theta=0, \pi$$

SC loop containing Josephson jns.	even	number of sign changes in I_s	0	integer	flux quantization
	odd		π	$\frac{1}{2}$ integer	

As a function of the loop geometry, the presence and absence of the $\frac{1}{2} \Phi_0$ effect can be used for probing the phase of the order parameter, $\Delta(\mathbf{k})$.

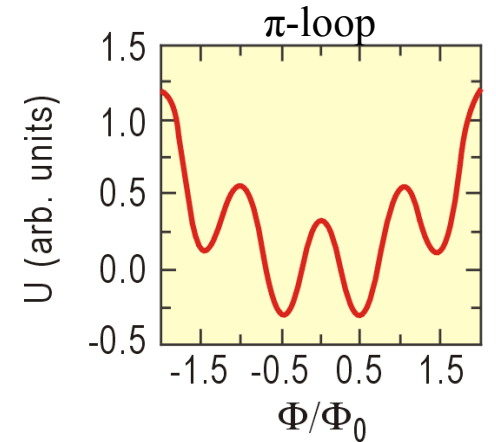
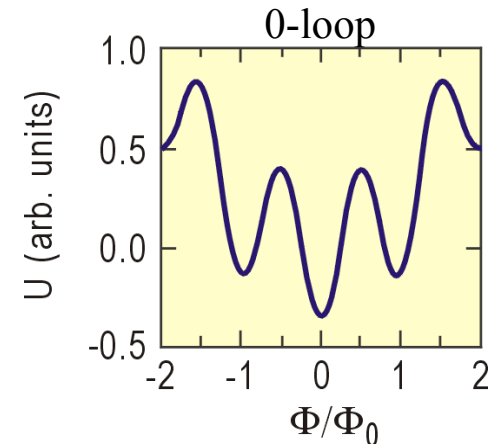
Techniques for observing the $\frac{1}{2} \Phi_0$ effect:

SQUID interferometry: Wollman, van Harlingen et al. (1993).
Brawner & Ott (1994), Mathai, ... Welstead (1995).

Josephson jn modulation: Wollman, van Harlingen et al. (1995).
Miller et al. (1995), Iguchi and Wen (1994)

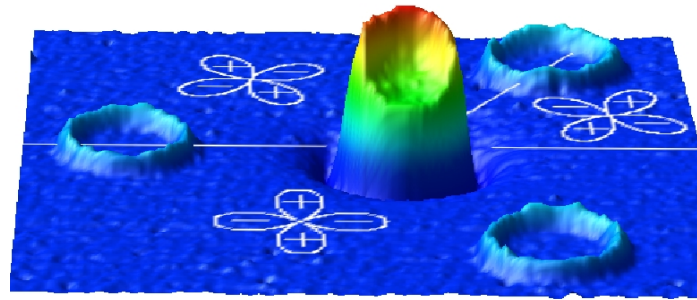
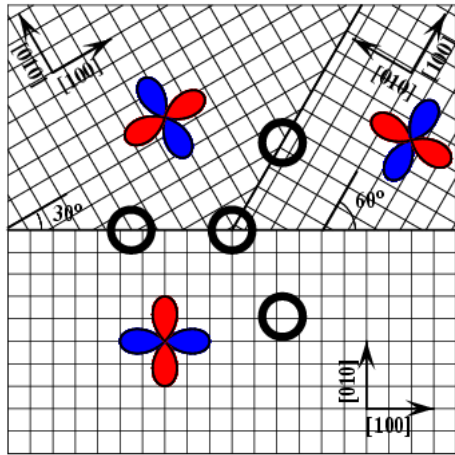
Tricrystal magnetometry: Tsuei, Kirtley et al. (1994)

Bulaevskii, Kuzii
& Sobyain (1977).
Geshrenbein, Larkin
& Barone (1987).
Sigrist & Rice (1992)

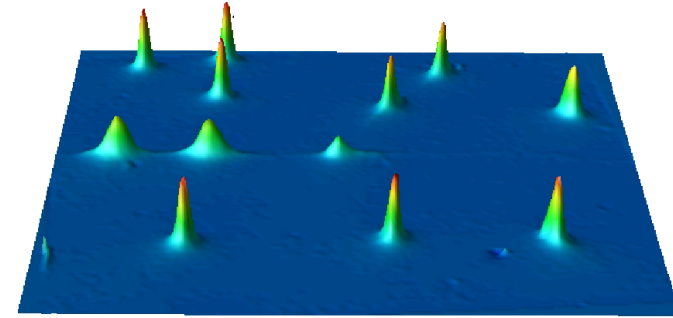


Tricrystal geometry

Scanning SQUID Microscope Images



C. C. Tsuei et al., PRL 73, 593 (1994)



J.R. Kirtley et al., PRL 76, 1336 (1996)

YBCO epitaxial film 4.2 K

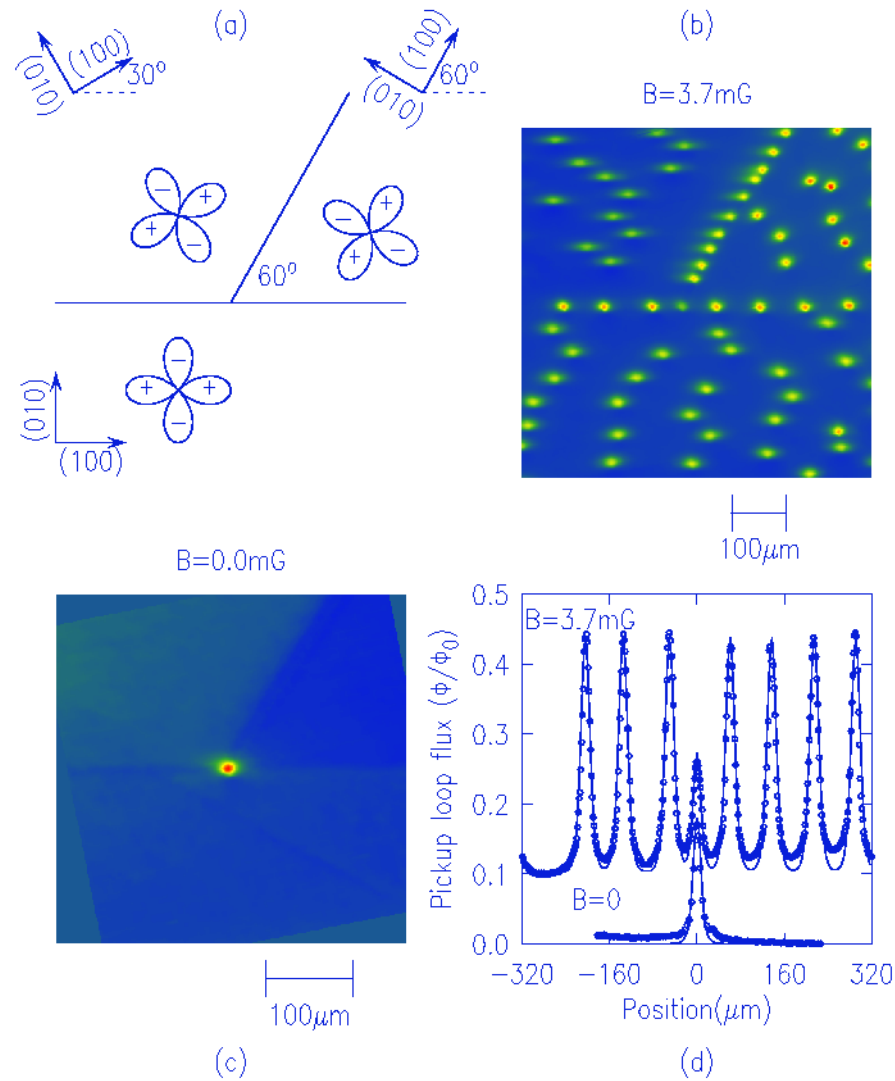
- effect of disorder at the gb junction interface was taken into consideration
- a yes or no pairing symmetry test.
- well – adapted for testing the gap symmetry of various cuprate superconductors, and especially the doping dependence of a particular cuprate system.

C.C. Tsuei and J.R. Kirtley, Rev. Mod. Phys. 72, 969 (2000)

The original tricrystal experiment was repeated and confirmed by A. Sugimoto et al.

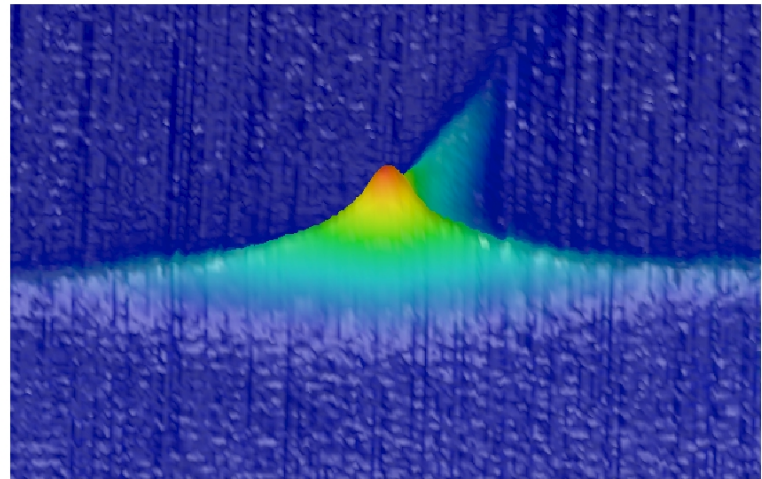
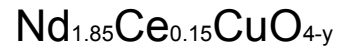
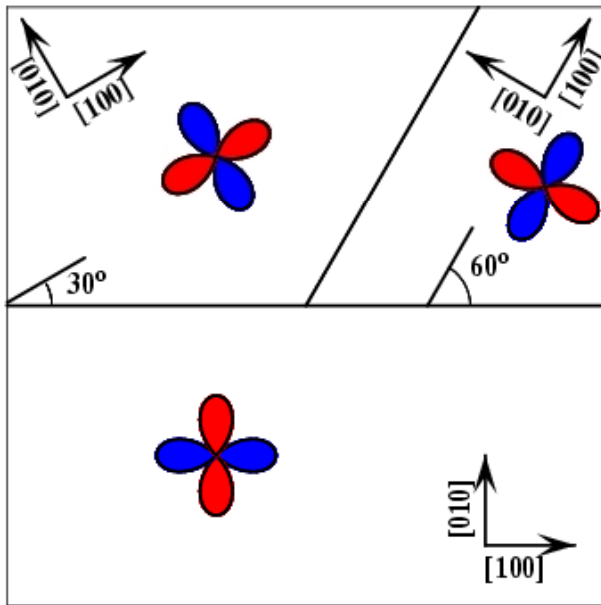
Physica C 367, 28 (2002).

$\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$



J.R. Kirtley, C.C. Tsuei, H. Raffy, Z.Z. Li, A. Gupta, J. Z. Sun, S. Megert,
Europhys. Lett. **36**, 707 (1996).

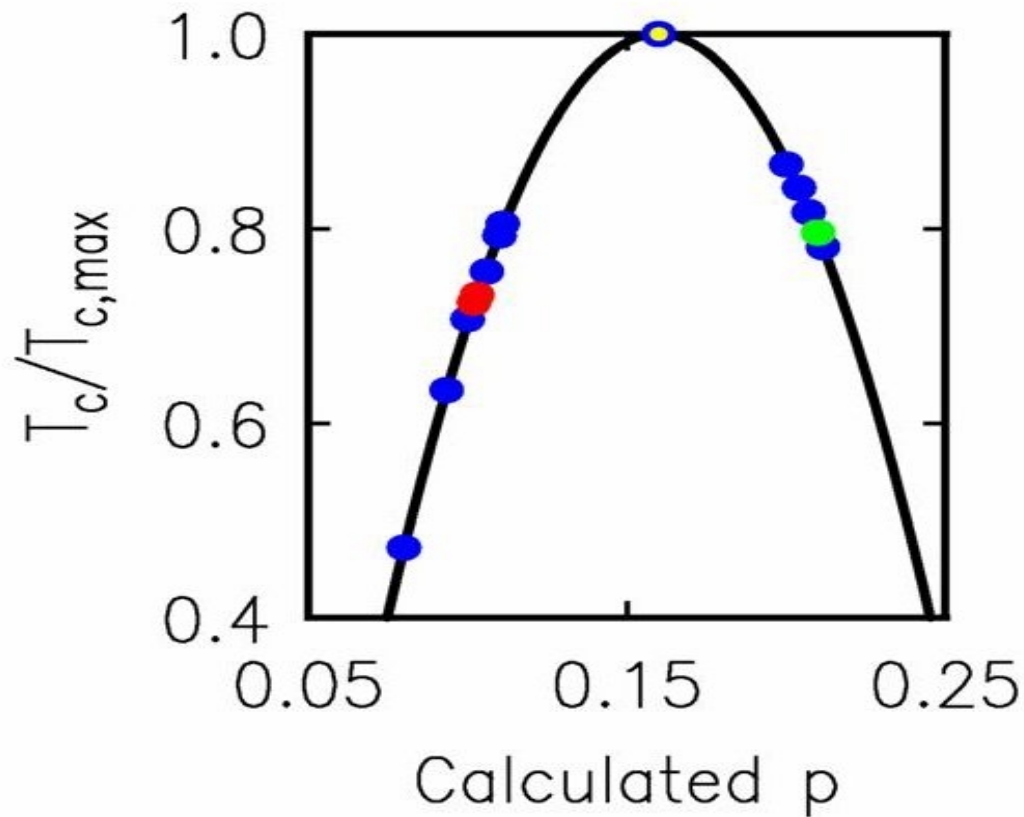
Tricrystal pairing symmetry tests of electron doped cuprates



C.C. Tsuei and J.R. Kirtley, PRL **85**, 182 (2000)

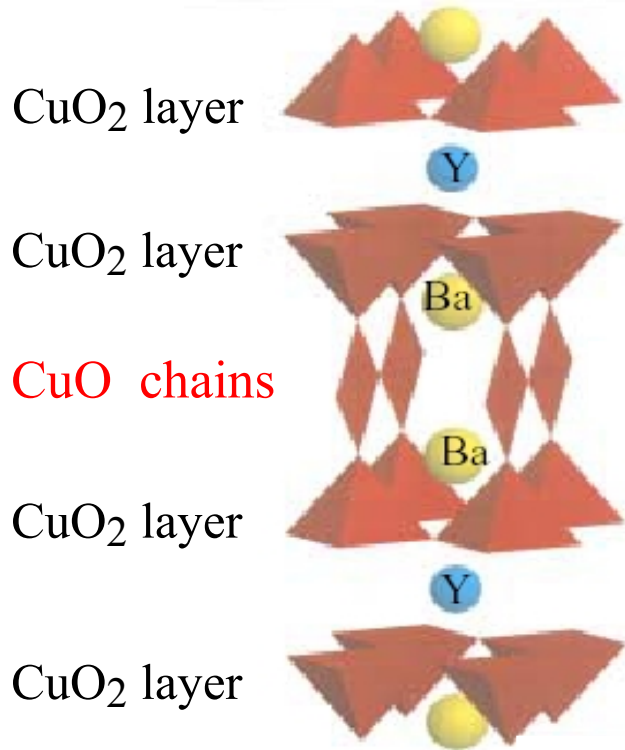
Doping Dependence of Pairing Symmetry

- LSCO
- BSCCO
- $Y_{1-x}Ca_xBa_2Cu_3O_{7-\delta}$



$T_c = T_{c,max} [1 - 82.6(p - 0.16)^2]$, M.R. Presland et al. *Physica C* **176C**, 95 (1991).

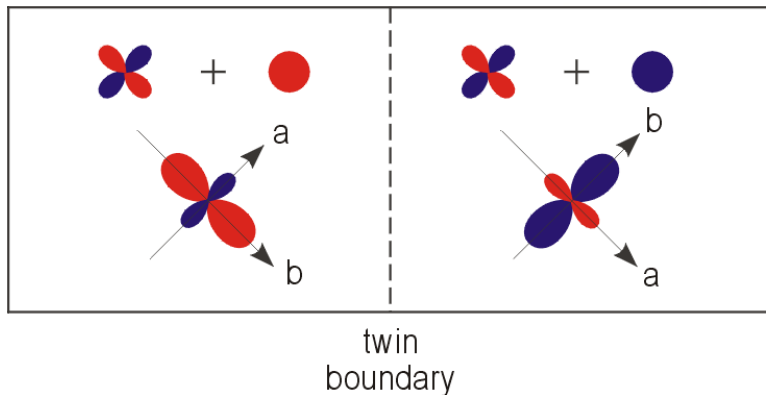
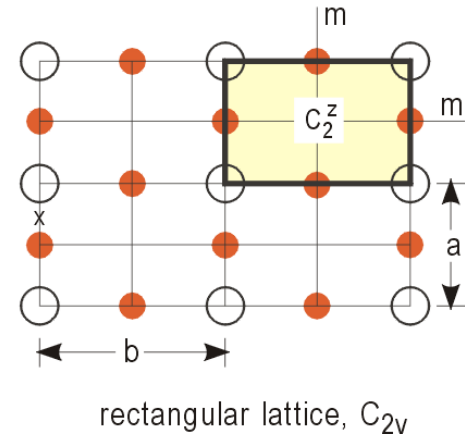
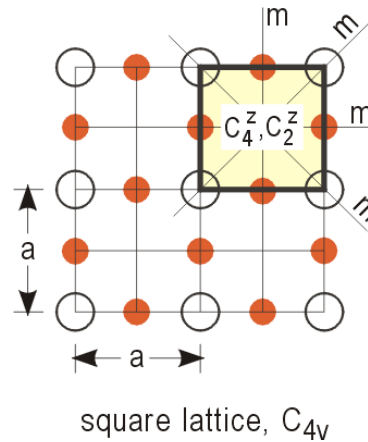
Crystal Structure and Allowed Pair States In YBCO



double CuO₂ planes plus Cu-O chains

Structure and point-group symmetry of the CuO₂ layer

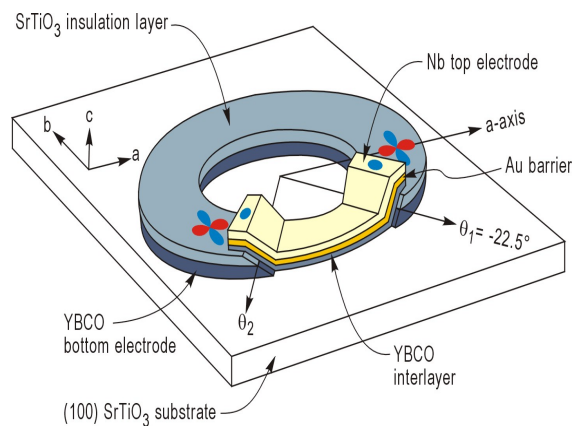
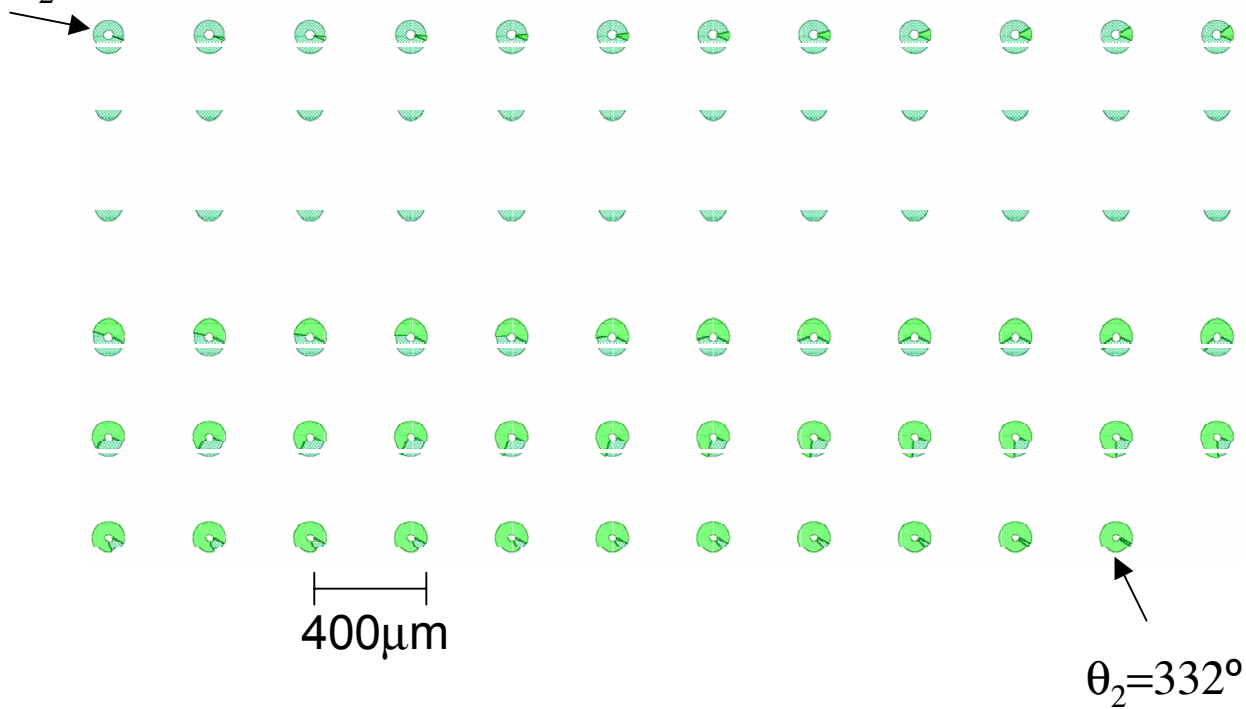
● = oxygen , ○ = copper



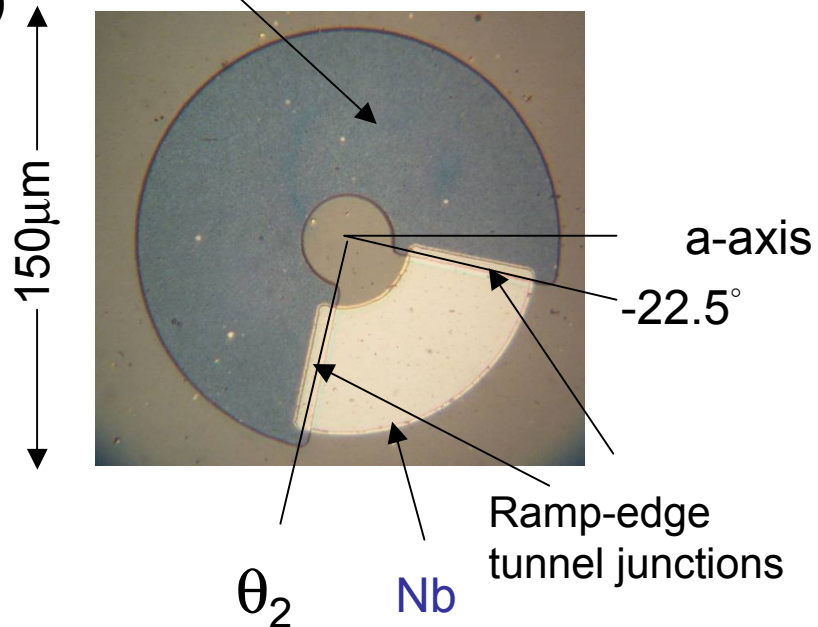
M. Walker, J.L-Strathmann PRB **54**, 588 (1996)

K. Kouznetsov et al. PRL **79** 3050 (1997)

(a)

 $\theta_2 = -17^\circ$ YBa2Cu3O7-delta

(b)



(c)

